

## **Mathematics**

#### **Lessons and Activities**

Rising 6th Grade (Spanish)

#### **Table of Contents**

#### **Management Guide Pages**

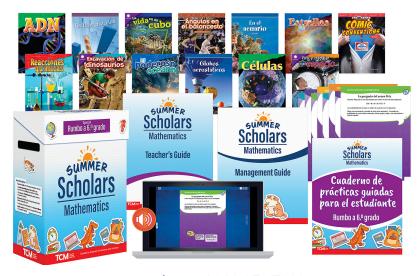
- Cover and Table of Contents (3 pages)
- How to Use This Resource (4 pages)
- Grade Level Details (8 pages)

#### Teacher's Guide Pages

- · Cover (1page)
- Days 3-4 Overview (1 page)
- Day 3 Lesson (5 pages)
- Day 4 Lesson (3 pages)

#### **Student Guided Practice Book Pages**

- Cover (1 page)
- Day 3 Student Pages (7 pages)
- Day 4 Student Pages (5 pages)





**Mathematics** 

# Management Guide



## **Table of Contents**

Welcome Letter	5
Overview	6
Effective Mathematics Intervention	6
Effective Mathematics Instruction for All Learners	7
Using Concrete Models	
Concrete-Representational-Abstract Instructional Sequence	
Math Fluency	10
Developing Mathematical Problem-Solving Skills	11
Why Teach Problem-Solving?	11
Making Connections	11
Problem-Solving Framework	11
Problem-Solving in Summer Scholars	13
Mathematical Practices/Processes	14
Promoting Mathematical Discourse in the Classroom	15
About the Routines	16
Understand and Plan Routine	16
Share and Discuss Routine	17
Reflect and Write Routine	17
Implementing the Routines	18
How to Introduce the Routines	18
Debriefing a Lesson	20
Introduction to STEAM Education	27
The Importance of STEAM Education	27
Defining STEAM	27
The Engineering Design Process	29
How to Facilitate Successful STEAM Challenges	30
Differentiation	32
Below-Level Support	32
Language Learner Support	32
Extend Learning	32
Using Summer Scholars	33
How to Use This Resource	33
What's Included?	
Scaffolded Mathematics Instruction	
Mathematical Discourse Task Cards	35
STEAM Challenges	
Classroom Library	
Assessment	
Digital Assessment in Summer Scholars	38

## Table of Contents (cont.)

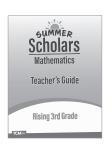
Technology	39
Digital Math Fluency Games	39
Interactive Ebooks	40
Audio Recordings	41
Additional Digital Resources	41
Planning Your Summer School Program	42
Pacing Plan Overview	42
Grade Level Details Overview	43
Grade Level Details	45
Rising 1st Grade	45
Scope and Sequence	46
STEAM Challenges and Materials	49
Classroom Library Information	50
Rising 2nd Grade	51
Scope and Sequence	52
STEAM Challenges and Materials	55
Classroom Library Information	56
Rising 3rd Grade	57
Scope and Sequence	58
STEAM Challenges and Materials	61
Classroom Library Information	62
Rising 4th Grade	63
Scope and Sequence	64
STEAM Challenges and Materials	67
Classroom Library Information	68
Rising 5th Grade	69
Scope and Sequence	70
STEAM Challenges and Materials	
Classroom Library Information	74
Rising 6th Grade	77
Scope and Sequence	78
STEAM Challenges and Materials	81
Classroom Library Information	83
References Cited	85
Accessing Digital Assessments	87
English Resources	87
Spanish Resources	87
Digital Resources	88
Accessing the Digital Resources	88
Contents of the Digital Resources	88

#### **How to Use This Resource**

The Summer Scholars Mathematics curriculum has been designed to meet the needs of summer learning programs. Scaffolded lessons, mathematical discourse, and STEAM activities are presented in a flexible format to make learning (and teaching) fun and effective for everyone.

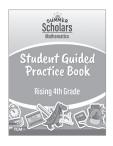
#### What's Included?

#### Teacher's Guide



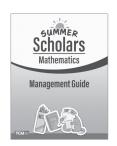
The daily lessons enhance instruction with research-based mathematics instructional practices.

#### **Student Guided Practice Book**



This book encourages students' mathematical fluency with multiple opportunities to apply learning.

#### **Management Guide**



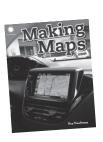
This guide helps teachers plan effectively with flexible lesson pacing and a scope and sequence designed specifically for varied summer settings.

#### 12 Mathematical Discourse Task Cards



These cards provide rich problem-solving tasks for students to solve and discuss collaboratively. They are provided in both print and digital format.

#### **Smithsonian STEAM Readers**







These books and the included STEAM challenges foster content-area literacy and encourage students to collaboratively solve real-world problems.

#### **Digital Resources**



These resources increase student engagement and enhance instruction. Family Engagement Letters are provided for a strong school-home connection.

#### **Classroom Library with 10 Books**

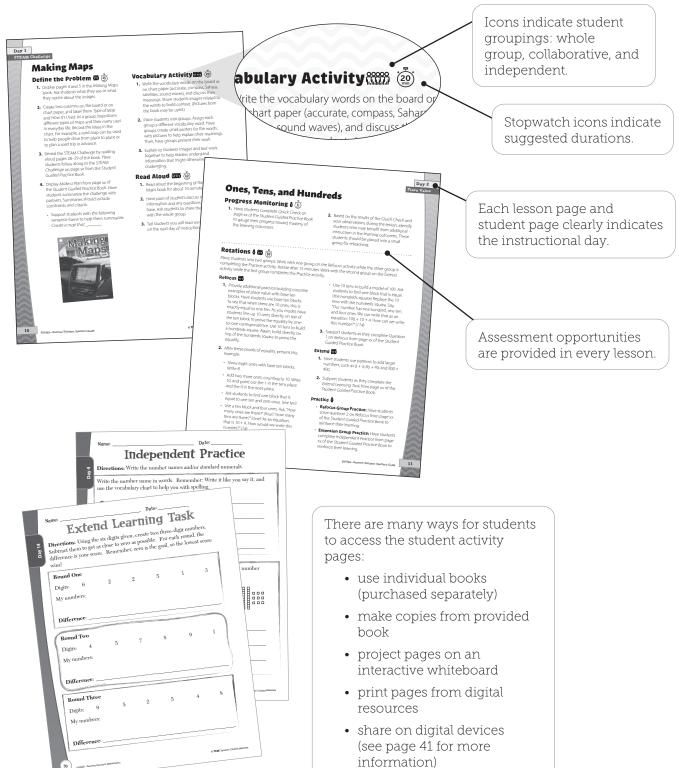


These mathematics- and science-focused books inspire curiosity and a love of reading.

## How to Use This Resource (cont.)

#### **Scaffolded Mathematics Instruction**

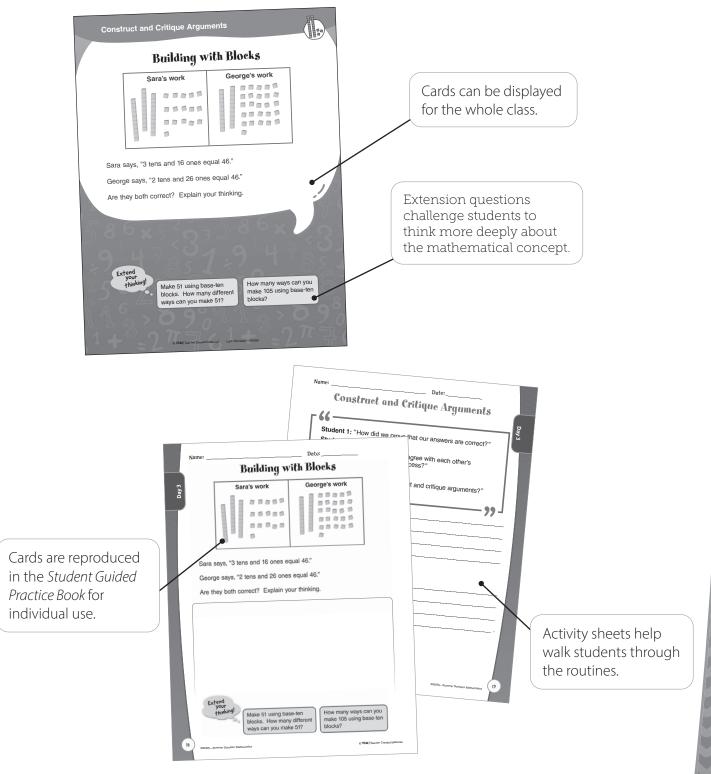
The student-centered Gradual Release of Responsibility model is embedded into each of the mathematics lessons. Within every two-day lesson, the responsibility shifts from the teacher (I Do) to the student (You Do).



#### How to Use This Resource (cont.)

#### **Mathematical Discourse Task Cards**

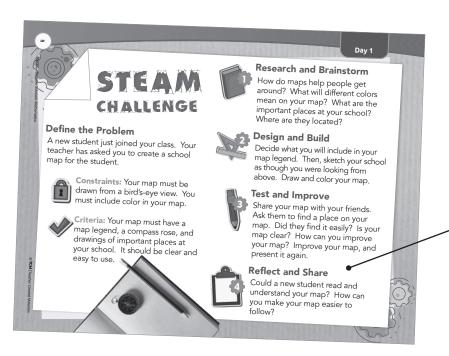
The Mathematical Discourse Task Cards present rich math problems for students to solve and discuss collaboratively. The three mathematical discourse routines walk students through the problem-solving process.



#### How to Use This Resource (cont.)

#### **STEAM Challenges**

There are five STEAM Challenges included in each level of *Summer Scholars*. Each challenge is completed over five days to give students ample time to investigate, test, and retest their ideas. In addition to meeting specific criteria, students are also challenged to improve their work over the five days.



Days 3-4 Overview

Numbers to 1,000 Learning Outcome

Student Misconception

Making Maps Learning Outcomes

**Building with Blocks** 

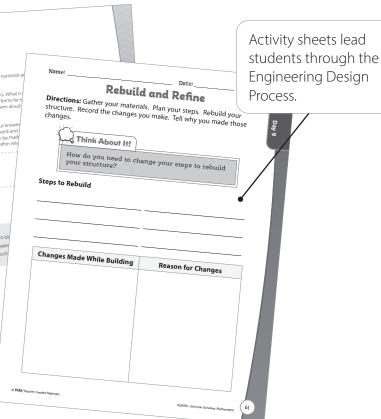
Book (pages xx-xx)

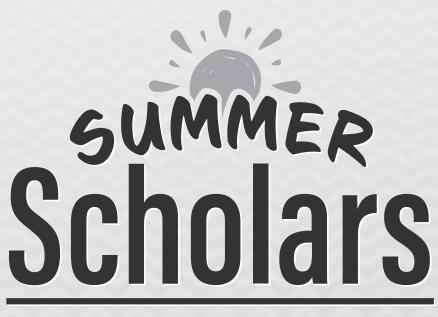
Number Name Cards
(wimname.pdf)

Build background knowledge and spark student interest with engaging readers and short texts.

Students reflect on the process and their final products.

Materials needed for each challenge are clearly listed. A full list of all STEAM Challenge materials is included in the digital resources.





**Mathematics** 

# Rising 6th Grade

**Grade Level Details** 

## **Rising 6th Grade Scope and Sequence**

	Mathematics Sk 60–65 min	Mathematics Skills and Concepts 60–65 minutes per day	<b>Problem-Solvin</b> 10–15 minu	<b>Problem-Solving and Discourse</b> 10–15 minutes per day	<b>STE</b> 45 minute	<b>STEAM</b> 45 minutes per day
	Mathematics Focus	Standards	Mathematical Practice and Card Title	Standard	Challenge Title and STEAM Step	Standard
Day 1	Using Parenthesis,	Evaluate multi-step numerical expressions using order of operations.	Use Tools Strategically	Consider and use available tools when	<i>Life in a Cube</i> Define the Problem	Convert among different-sized standard measurement units within a given
Day 2	Brackets, and Braces	including parenthesis, brackets, and braces.	"Mr. Petz's Question"	solving problems.	<i>Life in a Cube</i> Design	measurement system and use these conversions to solve real-world problems.
<b>Бау</b> 3	M/A disconsisted	Translate written real- world and mathematical problems into numerical	Analyze the Structure	Observe closely to	<i>Life in a Cube</i> Build and Test	Apply mathematics to solve problems arising in
Day 4	WORKING WITH EXPRESSIONS	expressions that record calculations with numbers.	"Ms. Suh's Math"	discern a patient of structure in a problem.	Life in a Cube Improve	everyday life, society, and the workplace.
Day 5		Compare and order		Use assumptions,	Life in a Cube Reflect and Share	Make sense of problems and plan, solve, justify and evaluate solutions.
Day 6	Comparing Decimals to the Thousandths	decifials to the thousandths using >, =, and < symbols to record the results of the comparisons.	Construct and Critique Arguments "Diana Disagrees"	definitions, and previously established results to construct arguments.	Gravity Learn Content, Understand the Challenge, and Brainstorm	Define gravity, identify how its forces affect life on Earth, and explore how these forces can be manipulated.
Day 7	Adding and Subtracting	Add and subtract numbers with decimals using strategies, like	Think Using Quantities	Make sense of quantities and their relationships in	Gravity Design and Build	Apply mathematics to solve problems arising in
Day 8	Decimals	the standard algorithm, based on place value and properties of operations.	"Larry's Leashes"	problems.	Gravity Test and Reflect	everyday life, society, and the workplace.

## Rising 6th Grade Scope and Sequence (cont.)

	Mathematics Ski 60–65 min	Mathematics Skills and Concepts 60–65 minutes per day	Problem-Solving 10–15 minu	<b>Problem-Solving and Discourse</b> 10–15 minutes per day	STEAM 45 minutes per day	AM es per day
	Mathematics Focus	Standards	Mathematical Practice and Card Title	Standard	Challenge Title and STEAM Step	Standard
Day 9	Multiplying Decimals	Represent the multiplication of numbers with decimals and multiply numbers with	Think Using Quantities "Magic or Math?"	Make sense of quantities and their relationships in	<i>Gravity</i> Redesign and Rebuild	Make sense of problems and plan, solve, justify
Day 10		decimals using strategies based on place value and properties of operations.		problems.	<i>Gravity</i> Retest and Share	and evaluate solutions.
Day 11		Divide numbers with decimals using strategies	Generalize Your Thinking	Look for and express	Digging Up Dinosaurs Define the Problem	Make sense of problems and plan, solve, justify and evaluate solutions.
Day 12	Dividing Decimals	based on place value and properties of operations with procedural reliability.	"Division Dilemma"	regulanty in repeated reasoning.	Digging Up Dinosaurs Design	Fluently multiply multidigit whole numbers using the standard algorithm.
Day 13	Adding and Subtracting Fractions (Unlike	Add and subtract fractions with unlike denominators that refer	Use Tools Strategically	Consider and use available tools when	Digging Up Dinosaurs Build and Test	Apply mathematics to solve problems arising in
Day 14	Denominators)	generating equivalent fractions.	. LIZ S Lettovers	solving problems.	Digging Up Dinosaurs Improve	the workplace.
Day 15		Extend previous understandings of			Digging Up Dinosaurs Reflect and Share	Make sense of problems and plan, solve, justify and evaluate solutions.
Day 16	Multiplying Fractions	represent and solve multiplication of a fraction by a whole number or another fraction.	Analyze the Structure "Richie's Ribbons"	Observe closely to discern a pattern or structure in a problem.	Bones and Skeletons Learn Content, Understand the Challenge, and Brainstorm	Create a model of a human skeleton to experiment with how humans bend their bodies.

## Rising 6th Grade Scope and Sequence (cont.)

	Mathematics Ski 60–65 min	Mathematics Skills and Concepts 60–65 minutes per day	<b>Problem-Solving and Discourse</b> 10–15 minutes per day	g and Discourse Ites per day	<b>STE</b> 45 minut	<b>STEAM</b> 45 minutes per day
	Mathematics Focus	Standards	Mathematical Practice and Card Title	Standard	Challenge Title and STEAM Step	Standard
Day 17	Dividing Fractions Dart	Interpret and represent division of a whole number by a unit fraction	Think Using Quantities	Make sense of quantities	<i>Bones and Skeletons</i> Design and Build	Apply mathematics to solve problems arising in
Day 18		and division of a unit fraction by a whole number.	"Leftovers"	problems.	Bones and Skeletons Test and Reflect	everyday life, society, and the workplace.
Day 19	Dividing Fractions, Part II	Extend previous understanding of division to divide a unit fraction	Use Tools Strategically	Consider and use available tools when	<i>Bones and Skeletons</i> Redesign and Rebuild	Make sense of problems and plan, solve, justify
Day 20		by a non-zero whole number.	"Brownies to Share"	solving problems.	Bones and Skeletons Retest and Share	and evaluate solutions.
Day 21		Determine volumes of			Living and Working in Space Define the Problem	Make sense of problems and plan, solve, justify and evaluate solutions.
Day 22	Finding Volume	with whole number side lengths by counting individual unit cubes or layers of unit cubes.	Generalize Your Thinking "Prism Patterns"	Look for and express regularity in repeated reasoning.	Living and Working in Space Design	Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.
Day 23	Locating and Plotting on	Understand and describe key attributes of the	Think Using Quantities	Make sense of quantities	<i>Living and Working in</i> Space Build and Test	Apply mathematics to solve problems arising in
Day 24	a Coordinate Plane	coordinate plane. Plot and label ordered pairs using the origin (0, 0).	"What's the Point?"	and their relationships in problems.	<i>Living and Working in</i> Space Improve	everyday life, society, and the workplace.
Day 25	Culminating Activity				Living and Working in Space	Make sense of problems and plan, solve, justify
					Reflect and Share	and evaluate solutions.

## Rising 6th Grade STEAM Challenges and Materials

This chart includes descriptions and needed materials for the five STEAM Challenges.

Challenge Name	Description	Materials
Life in a Cube (reader)	Teams re-create cubes similar to the one photographer David Liittschwager used to observe various habitats.	<ul> <li>classroom supplies     (construction paper,     glue, markers) <ul> <li>aluminum foil</li> <li>cardboard pieces     and tubes</li> <li>masking tape</li> <li>newspaper</li> <li>paint</li> <li>plastic wrap</li> <li>spray bottle</li> </ul> </li> </ul>
Gravity	Students create devices that slow a package as it falls.	<ul> <li>books or online resources about helicopter seeds, animals, and parachutes</li> <li>calculator</li> <li>fabric (various types)</li> <li>plastic wrap</li> <li>small box or another object weighing about 1 oz. (30 g)</li> <li>stopwatch</li> <li>string/yarn (3–4 ft, 1 m)</li> </ul>
Digging Up Dinosaurs (reader)	Teams create displays that can present dinosaur skeletons.	<ul> <li>cardboard pieces</li> <li>construction paper</li> <li>modeling clay</li> <li>cotton swabs</li> <li>paper-mache materials</li> <li>cue tips</li> <li>foil</li> <li>masking tape</li> <li>modeling clay</li> <li>paper-mache materials</li> <li>pipe cleaners</li> <li>scissors</li> </ul>

## Rising 6th Grade STEAM Challenges and Materials (cont.)

Challenge Name	Description			
Bones and Skeletons	Students create simple model hands with fingers that can move.	<ul> <li>cardboard sheets (2-3) <ul> <li>cardstock</li> <li>craft sticks (5-10)</li> <li>disposable gloves (2)</li> <li>fishing line (3-4 ft., 1 m)</li> <li>modeling clay</li> <li>pipe cleaners (10-15)</li> <li>wire (different gauges; optional)</li> <li>yarn (3-4 ft., 1 m)</li> </ul> </li> </ul>		
Living and Working in Space (reader)	Teams design and build specialized tools that improve the daily lives of astronauts in microgravity.	<ul> <li>cardboard pieces</li> <li>pipe cleaners</li> <li>rubber bands</li> <li>craft sticks and tubes</li> <li>masking tape</li> <li>paper cups</li> </ul>		

## **Rising 6th Grade Classroom Library Information**

This chart includes important information about the books included in the classroom library.

Book Title	Lexile® Measure	*Guided Reading Level	Summary
At the Aquarium	840L	V	Get a behind-the-scenes look at how an aquarium functions. Discover and learn about different kinds of marine life while studying the sizes, shapes, and volumes of tanks. Learn how to measure volume by weighing aquarium animals and determining how much food they need to eat.
Basketball Angles	780L	U	Learn about angles through the fast-paced sport of basketball! Explore where angles exist in basketball strategies, such as dribbling, shooting, passing, and rebounding the ball. Discover how predicting angles can help you become a better basketball player!
Cells	770L	X	You can't see them, but every living thing is made of cells. They are the building blocks of life. And each cell has a specific function. What do the cells in your blood do? What about the cells in your eyes? You might be surprised to learn how these tiny cells have such important duties.
Chemical Reactions	720L	Υ	Dynamite is highly explosive. This is because it's a chemical reaction waiting to happen. Many things go through chemical reactions. When you cook or eat, a chemical reaction takes place. Understanding chemical reactions will not only keep you safe, but it will also help reveal the world around you.
DNA	820L	Υ	Twins can look identical. And siblings or children may look similar to other people in their family. Even kittens can have the same markings as other kittens in a litter. But why? The answer is DNA. DNA is what makes family members look similar but also makes them unique. DNA is what makes you, well, you!
Comic Conventions: Division	790L	Т	Join Zach as he visits a comic convention and finds out why "fans" is short for "fanatics"! Show off your strategies for division as the crowds show off their love for comic books, movies, and characters.

## Rising 6th Grade Classroom Library Information (cont.)

Book Title	Lexile® Measure	*Guided Reading Level	Summary
Graphs in Action	770L	S	Explore the world of graphs! Learn how to create bar graphs, line graphs, pictographs, and circle graphs.  Discover how graphs are labeled and can visually organize information. Then, create your own graphs.
Hot Air Balloons	830L	V	Have you ever wondered how hot air balloons work? Discover the mechanics of hot air balloons while also learning how to calculate the volume of a balloon and its basket. Explore how volume has real-world applications.
Stars	860L	V	Stars light up the sky on a clear night. They may look the same from Earth, but they come in many sizes and colors. Some stars are closer to Earth than others. Some are old, and some are young. Even though stars are so far away, learning about them helps us to better understand the world around us.
The Powerful Ocean	780L	V	The ocean is beautiful, powerful, and refreshing. The salty water provides the perfect home for many plants and animals. Within these waters are choppy currents and strong tides. But without the ocean, our world would be a very different place.

<sup>\*</sup>These titles have been officially leveled using the F&P Text Level Gradient™ Leveling System.



**Mathematics** 

Teacher's Guide

Rising 6th Grade



### Days 3-4 Overview

#### **Working with Expressions**

#### **Learning Outcome**

• Write simple expressions that record calculations with numbers and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and 7, then multiply by 2" as  $2 \times (8 + 7)$ . Recognize that  $3 \times (18,932 + 921)$  is three times as large as 18,932 + 921, without having to calculate the indicated sum or product.

#### **Focus**

The following lesson will address this focus question: *How do you write a numerical expression?* You may wish to write the focus question on the board or chart paper and read it aloud to students.

#### **Student Misconceptions**

Students often do not understand the difference between the terms expression and equation. They may use the two terms interchangeably. An equation results when two expressions are equivalent or equal. For example,  $3 \times 8 = 6 \times 4$  and  $4 = 24 \div 6$  are equations. An expression includes numbers and operational symbols but does not contain an equal sign. An easy way to teach the difference is to point out that the term equation contains most of the word equal; therefore, it needs an equal sign.

#### **Mathematical Discourse**

#### **Learning Outcome**

• Look for and make use of structure while solving math problems. Understand that analyzing structure means to look at how the mathematics in the task is organized to solve.

#### Life in a Cube

#### **Learning Outcome**

• Use mathematical knowledge to build and improve upon an engineering design.

#### **Materials**

- Student Guided Practice Book (pages 16–27)
- Ms. Suh's Math Question task card
- Life in a Cube book
- index cards

#### **Materials per STEAM Group**

- classroom supplies (construction paper, glue, markers)
- aluminum foil

- cardboard pieces and tubes
- craft sticks
- masking tape
- newspaper

- paint
- plastic wrap
- spray bottle

### Warm-Up (10)

- 1. Say, "Today, you will be practicing using the Order of Operations by creating your own expressions and making a clock face. You will use the number 4 to create expressions that equal the numbers 1–12. You can only write the number 4 four times in each expression. Remember to use the correct order of operations to solve the problems: Parentheses, Exponents, Multiply, Divide, Add, or Subtract.
- 2. Show students an example. Say, "In the expression  $4 \times (4 \div 4) + 4$ , the first step I need to complete is to solve inside the parentheses. The second step is to multiply, and the last step is to add." Show the steps on the board or chart paper. Say, "Since the solution is 8, I am going to write that expression on my clock where the number 8 is." Draw a clock by making a circle on the board or chart paper, and write the expression  $4 \times (4 \div 4) + 4$  in place of the 8.
- **3.** Allow students time to work with partners to complete their clocks. Have students share their expressions to confirm their answers.

#### Language and Vocabulary



**1.** Write the following vocabulary terms on the board or chart paper. Review the definition of each term with the class.

equation evaluate

expression

- 2. Explain to students that they will create a visual image for each word to help them remember its meaning. Begin with the word equation. Say, "Equations are number sentences that include an equal sign and a value on either side of the equal sign." Ask students to think of a relevant visual image that goes with this word. Direct the discussion toward the use of an equal sign. Draw an equal sign on the board or chart paper.
- 3. Now, do the same with the word *expression*. Say, "An expression is a number sentence that does not have an equal sign." Ask students to think of a relevant visual image. If students do not have any ideas, suggest an equal sign circled with a line through it.
- **4.** Conclude with the word *evaluate*. Say, "In math, you may be asked to evaluate a problem. This means to simplify or solve the problem." Ask students to think of a relevant visual image that goes with this word. The letter *S* may help them to remember that *evaluate* means "to simplify or solve."
- **5.** Show examples of expressions and equations. Ask students to state whether the example is an expression or an equation. Examples may include:

$$(10 \div 2) + 5$$
  
 $25 - (6 + 3) = 2 \times 8$   
 $4 \times 2 + (6 \div 3)$   
 $(60 + 24) \div 4 = 3 \times 7$ 

## I Do com (10)

- **1.** Say, "Today, we are going to write mathematical expressions. Here is an example: Add 5 and 6 together. Then, multiply the sum by 2." Say, "Write an expression that uses numbers and symbols to represent these two sentences." Allow time for students to write an expression. Observe students' answers.
- **2.** Write  $5 + 6 \times 2$  on the board or chart paper. Say, "I noticed that some of you wrote this expression. This makes sense as we follow what the words say. First, it says to add 5 and 6. Then, it says to multiply by 2." As you talk, point to each part of the sentence and the expression to make a connection between the two representations.
- **3.** Say, "I remember that the Order of Operations says we must multiply *before* we add. In this problem, I must multiply 6 times 2, and then add 5. But that is not what the words say to do."
- **4.** Ask, "What can I do to make sure that we add before we multiply?" Allow for student responses. If students do not suggest that parentheses are needed, ask, "What mathematical symbol is used to indicate that part of the expression needs to be completed first?" Add parentheses to the expression:  $(5+6) \times 2$ . Then, say, "The parentheses show I need to add 5 and 6 together first. Then, I need to multiply the sum by 2." Ask, "Is there another way I can write this expression?"  $(2 \times (5+6) \text{ or } 2(5+6))$

- **5.** Say, "Let's do another example: *Divide 16* and 8. Then, double it. Have students write the expression. Ask for volunteers to write their expression on the board or chart paper, and have the class agree or disagree by giving a thumbs-up or thumbs-down. Ask if any students wrote the expression a different way and have them present their expression on the board or chart paper. Students may have suggested  $(16 \div 8) \times 2$  or  $2 \times (16 \div 8)$  or  $2(16 \div 8)$ .
- **6.** Next, write the expression  $25 \times (104 + 246)$  on the board or chart paper. Say, "I don't want you to solve or evaluate this expression. Instead, I want you to interpret the expression. Tell your partner what the expression means." Allow time for students to discuss the meaning of the expression. Have students share their responses. Students should indicate that the parentheses tell them to add first. The solution will be 25 times greater than the sum. Say, "The reason we are interpreting the expression and not solving it is to get practice in understanding the meaning of the expression before solving. If we understand what we are doing before doing it, we know if our solution is reasonable."

## We Do (15)

- 1. Display Expressive Expressions from page 16 of the Student Guided Practice Book.
  Say, "Let's look at some more expressions together." First, read Question 1: Add seven and two. Multiply the sum by four.
- 2. Ask, "How can we write this expression to make sure we calculate it in the correct order?" Allow students to write the expression on their activity sheets. Provide specific feedback to students, such as "I notice you have 7 + 2 × 4. That is the order of the wording in the problem, but the Order of Operations tells us that we must multiply before adding. How can you make sure the addition expression is completed first? Is there a grouping symbol you could use? Which one?"

Support for Language Learners: As you work through this lesson, provide each student an index card with relevant math vocabulary and symbols recorded on it. For example: sum, add, plus; difference, minus, subtract; product, times; quotient, divide. To further support students' vocabulary development, you can display these words on a word wall with their definitions and examples. It may also be helpful to list the relevant grouping symbols students will use on the board or chart paper.

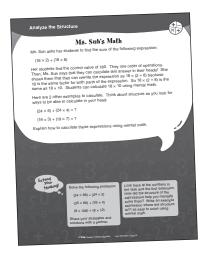
- **3.** Have students explain their solution for Question 1. To help students explain their reasoning, provide them with the following sentence frames:
  - In this problem, the \_\_\_\_\_ and the \_\_\_\_\_ need to be calculated first.
  - I can represent this by putting those numbers and the operation in \_\_\_\_\_\_.
  - After I find the \_\_\_\_\_, then I have to

- **4.** Repeat Steps 1–3 for Question 2: Four times the difference of five and two.
- **5.** Ask students to study the expression in Question 3:  $(12-6) \div 3$ . Say, "We are not going to solve this problem. Instead, we will interpret what it means." Have students discuss the expression with their partner. Ask students to share their interpretations. Write a sample response on the board or chart paper: First, we need to find the difference of 6 from 12. Then, we divide the difference by 3. The solution will be  $\frac{1}{3}$  of the difference.
- **6.** Have students explain their reasoning for Question 3. To help students explain their reasoning, provide them with the following sentence frames:
  - First, calculate what is in the \_\_\_\_\_ and find the difference.
  - Next, \_\_\_\_ the difference by 3.
  - The solution to the expression will be a of the difference.
- **7.** Repeat Step 6 for Question 4: 3 × (2,489 + 1,321).

## You Do 🖁 🗓

- **1.** Display *Examining Expressions* from page 17 of the *Student Guided Practice Book*. Provide the sentence frames from Steps 3 and 6 of the We Do section to help students explain their reasoning.
- 2. Have students share their expressions and reasoning. If students have difficulty explaining their reasoning, remind them to use the sentence frames and vocabulary terms.

## **Analyze the Structure**



#### **Understand the Strategy**

The Analyze the Structure practice or process stems from *look for and make use of structure*. As this practice or process is introduced, it is important that students understand that analyzing structure is about looking at how the mathematics in the task is organized and using that to make the task easier to solve. For example, students might reorder addends into friendly numbers or rearrange a shape to resemble another shape to find its area. These tasks have been written strategically to elicit student thinking around numerical and geometric relationships, the properties of numbers, and applying strategies which they've used before.

### Procedure n (15)

- 1. Display the *Ms. Suh's Math* task card and read aloud the text. Remind students to use the Understand and Plan, Share and Discuss, and Reflect and Write routines as they work through the task. Review these routines if needed. (See pages 21–26 in the *Management Guide*.)
- 2. Allow time for students to collaborate with partners as they follow the routines and work through the task from pages 18–19 of the *Student Guided Practice Book*. (Students will complete the extensions on the next day.)

**Answer:**  $(24 \times 6) + (24 \times 4) = 24 \times 10 = 240$  $(19 \times 3) + (19 \times 7) = 19 \times 10 = 190$ 

**Possible Misconception:** Students may think that the order of operations is the only approach to these expressions.

#### **Language Support**

- Tier 3: order of operations, calculate
- **Tier 2:** value, structure, expressions

#### Scaffolding

Ask students to solve this expression:  $3 \times (4 + 2)$ . Have them compare their approaches. If they all add (4 + 2) first, ask them to multiply  $(3 \times 4) + (3 \times 2)$ . Ask them to consider how these two approaches arrive at the same solution.

#### Life in a Cube

#### **Materials and Preparation**

• Prepare supplies for groups to use while building (construction paper, glue, markers, aluminum foil, cardboard pieces and tubes, craft sticks, masking tape, newspaper, paint, plastic wrap, spray bottle).

#### Read Aloud (1997) (5)



- **1.** Review the information from the previous day's read aloud.
- 2. Read another section of the Life in a Cube book. Pause periodically to discuss new information and any questions students may have.

## Build ## (30)

- **1.** Have groups review their *Collaborative* Design from page 15 of the Student Guided Practice Book. Explain to students that when they work with their groups to build the cubes, they must follow their team's design plans. Reassure them that they will have an opportunity to change and improve their designs after they present them.
- 2. Review classroom expectations for working with materials. Then, give teams time to build their cubes.
- **3.** Have students complete questions one and two on *Think about It* from page 20 of the Student Guided Practice Book. Explain that reflection is an important part of the engineering design process. After students have completed Think about It, ask volunteers to share their responses.

**Teacher Tip:** The students will test their cubes for durability. To create a more authentic experience for the Life in a Cube challenge, consider setting the cubes outdoors before the start of Day 5 and bringing students outside during STEAM to observe life in their cubes.

## Test 🞬 🗓

- 1. Gather teams for testing. Have teams transport their cubes to the testing location. Tell students they will test whether their cubes are waterproof and durable.
- 2. Explain that teams will offer feedback after each test. Use Friendly Feedback from page 21 of the Student Guided Practice Book to review best practices for giving feedback.
- **3.** Display Cube Test Results from page 22 of the Student Guided Practice Book. Ask students to record results for each team.
- **4.** Give time for each team to test. Ask a member of each group to explain how their models blend into the environment. Ask another member of the group to spray the cube with water and drop the cube from 1 meter (3 feet) high. A successful design blends in with the environment and survives the durability tests.
- **5.** Tell students that teams will brainstorm ways to improve their designs on the next day of instruction.

#### Progress Monitoring & 5

- **1.** Have students complete *Quick Check* from page 23 of the *Student Guided Practice Book* to gauge student progress toward mastery of the learning outcomes.
- 2. Based on the results of the *Quick Check* and your observations during the lesson, identify students who may benefit from additional instruction in the learning outcomes. These students should be placed in a small group for reteaching.

## Rotations 🛗 🖁 🗓

Place students in two groups. Work with one group on the Refocus activity while the other group is completing the Practice activity. Rotate after 15 minutes. Work with the second group on the Extend activity while the first group completes the Practice activity.

#### Refocus 🔐

- 1. Say, "Let's practice writing expressions by matching the words to the correct expression." Read the following words: the sum of six and three multiplied by two. Write the following expressions on the board or chart paper:  $2 \times (6+3)$  and  $6+3 \times 2$ . Ask students to choose which expression matches the words and to explain their thinking. Students should choose  $2 \times (6+3)$  and explain that first they need to add 6 and 3, and then multiply the sum by 2.
- **2.** Write the following expression on the board or chart paper:  $5 \times (4 + 3)$ . Ask, "How could we write this expression in words?" Provide words like *first*, *second*, *then*, or *next* to guide students to see that there is an order to solving the problem. Together, write the expression in word form. For example: *The sum of four and three multiplied by five*.
- **3.** Support students as they complete Question 1 on *Refocus* from page 24 of the *Student Guided Practice Book*, and then have them solve Question 2 independently.

#### Extend 员

- **1.** Write on the board or chart paper:  $\{4 + [(0+5) \times 3]\} \times 2$ . Remind students that when there is more than one grouping symbol, they need to work from the inside to the outside of the expression, starting with the parentheses. Work together to interpret the expression.
- **2.** Support students as they complete the *Extend Learning Task* from page 25 of the *Student Guided Practice Book.*

#### Practice မှိ

- **Refocus Group Practice:** Have students complete the questions on *Refocus* from page 24 of the *Student Guided Practice Book* to reinforce their learning.
- Extension Group Practice: Have students complete *Independent Practice* from page 26 of the *Student Guided Practice Book*.

#### Math in the Real World ### ## (25)

- 1. Display Math in the Real World: Double
  Day for Dogs from page 27 of the Student
  Guided Practice Book. Have a student read
  the task aloud. Tell students to explain or
  summarize the task to their partners. Have a
  few students share their summaries.
- 2. Ask students to think about what information they need to solve the task and what the task is asking them to do. Then, have them share with partners. Ask a few students to share aloud. Students should identify that they know Finnegan bought 5 bags of Mutt's Mix and 3 Doggie Donuts. Then, he got 5 more bags and 3 more donuts for free. Students need to find out if Finnegan's expression is correct. Have students work in groups of two or three to complete the task.
- **3.** As students are working, circulate and ask focusing, assessing, and advancing questions:
  - What information do you know?
  - How can you use this information in a mathematical expression?
  - How can you explain your reasoning?

**Support for Language Learners:** Share these sentence frames to help students explain their reasoning.

- Finnegan is/is not correct because \_\_\_\_\_
- In this problem, he did/did not include the correct numbers and operations.
- He did/did not put the problem in the correct order. I know this because

- 4. Observe how students are solving the task, and choose a few groups who solved the task in different ways to share their solutions and reasoning. Try to have solutions move from concrete to abstract representations. For example, have students share solutions with a visual representation (drawing), and then the symbolic representation (expression). Make sure students explain their reasoning as they share solutions.
- **5.** As groups are sharing their solution paths, reasoning, and strategies, ask questions:
  - Do you agree or disagree with the solution path and reasoning? Why?
  - Who can restate \_\_\_\_\_'s strategy/solution path/reasoning?
  - Which solution path makes the most sense to you? Why?

## **Analyze the Structure**

### Mathematical Discourse Card Extensions 🗯 🗓

- 1. Allow time for students to complete the routines for the Ms. Suh's Math task from the previous day.
- 2. Have students work in pairs to complete the extensions.
  - Solve the following problems:  $(24 \times 98)$  $+(24 \times 2); (35 \times 96) + (35 \times 4); (8 \times 108)$ + (8  $\times$  12). Share your strategies and solutions with partners. (2,400; 3,500; 960)
- Look back at the numbers in the task and the first extension. How did the structure of the expressions help you mentally solve them? Write an example expression where the structure isn't as easy to solve using mental math.

STEAM Challenge

#### Life in a Cube

#### **Materials and Preparation**

• Prepare supplies for students to use while rebuilding their cubes (construction paper, glue, markers, aluminum foil, cardboard pieces and tubes, craft sticks, masking tape, newspaper, paint, plastic wrap, spray bottle).

#### Read Aloud (5)



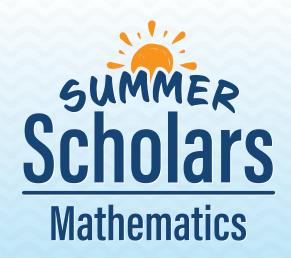
- 1. Review the information from the previous day's read aloud.
- **2.** Read pages of the *Life in a Cube* book for about five minutes. Pause periodically to discuss new information and any questions students may have.

## Improve ## (40)

- **1.** Have teams review the feedback they received on the previous day of instruction.
- **2.** Provide time for teams to brainstorm ways to improve their designs based on test results and feedback. Refer students back to Collaborative Design from page 15 of the Student Guided Practice Book. Ask them to sketch their improved designs and explain any changes. Have students submit improved designs for approval before building.

- **3.** Have teams gather materials to improve their designs. Then, have them retest their model cubes.
- **4.** Have students answer numbers 3–4 on Think about It from page 20 of the Student Guided Practice Book to reflect.

**Teacher Tip:** To create a more authentic experience for the Life in a Cube challenge, consider setting the cubes outdoors before the start of Day 5 and bringing students outside during STEAM to observe life in their cubes.



# Cuaderno de prácticas guiadas para el estudiante

Rumbo a 6.º grado



## Expresiones expresivas

**Instrucciones:** Escribe una expresión que coincida con las palabras. Luego, explica tu respuesta.

1 Suma siete más dos. Multiplica la suma por cuatro.

Expresión:

- **Explica:** \_\_\_\_\_\_
- Cuatro veces la diferencia de cinco y dos Expresión:
- Explica:

**Instrucciones:** Interpreta el significado de la expresión. Después, explica tu razonamiento.

 $(12-6) \div 3$ 

Significado:

Explica:

 $4 3 \times (2,489 + 1,321)$ 

Significado:

**Explica:** \_\_\_\_\_\_

# Examinar expresiones

**Instrucciones:** Escribe una expresión que coincida con las palabras. Después, explica tu respuesta.

Resta cinco de nueve. Suma dos a la diferencia.

Expresión:



2 Multiplica la suma de tres y seis por cinco.

Expresión:



Instrucciones: Interpreta el significado de la expresión. Después, explica tu razonamiento.

 $3 \times (1 + 7)$ 

Significado:



4  $(5,348 - 3,268) \times 2$ 

Significado:

**Explica:** \_\_\_\_\_\_

# +-

## Las matemáticas de la Srta. Suh

La Srta. Suh les pide a sus estudiantes que hallen la suma de la siguiente expresión:

$$(18 \times 2) + (18 \times 8)$$

Sus estudiantes hallan el valor correcto de 180. Usan el orden de las operaciones. Luego, la Srta. Suh les dice que ¡pueden calcular esta respuesta mentalmente! Les muestra que pueden reescribir la expresión como  $18 \times (2+8)$  porque 18 es el mismo factor para ambas partes de la expresión. Entonces,  $18 \times (2+8)$  es lo mismo que  $18 \times 10$ . Los estudiantes pueden calcular  $18 \times 10$  usando cálculo mental.

Aquí hay otros 2 ejemplos para calcular. Piensa en la estructura mientras buscas formas de poder calcular mentalmente.

$$(24 \times 6) + (24 \times 4) = ?$$

$$(19 \times 3) + (19 \times 7) = ?$$

iAmplia tu razonamiento!

135917—Summer Scholars: Mathematics—Spanish

Resuelve los siguientes problemas:

$$(24 \times 98) + (24 \times 2)$$

$$(35 \times 96) + (35 \times 4)$$

$$(8 \times 108) + (8 \times 12)$$

Comparte tus estrategias y soluciones con un compañero.

Vuelve a mirar los números de la tarea y la primera ampliación. ¿Cómo te ayudó la estructura de las expresiones a resolverlas mentalmente? Escribe un ejemplo de expresión cuya estructura no sea tan fácil de resolver usando cálculo mental.

## Analiza la estructura

6	6

### Reflexiona y escribe

Estudiante 1: "¿Qué buscamos para hacer más fácil la tarea?".

**Estudiante 2:** Responde.

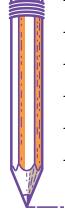
Estudiante 2: "¿Cómo aplicamos lo que sabemos para

ayudarnos?".

**Estudiante 1:** Responde.

Ambos piensan: "¿Cómo analizamos la estructura en esta tarea?".

Ambos escriben:	Para analizar la estructura,



Nombre:	Fecha:
---------	--------

## Piénsalo

I.	¿Qué problemas tuvo que enfrentar tu equipo? ¿Cómo los resolvieron?
2.	¿Qué hiciste para ayudar en tu equipo?
	¿Cómo usaste las ciencias, la tecnología, la ingeniería, las artes y/o las matemáticas en tus diseños?
4.	¿Qué salió bien en tu primer diseño? ¿Cómo lo mejoraste?
<b>5</b> .	¿Qué es lo más importante que aprendiste? ¿Qué preguntas te quedan?

Nombre:	Fecha:	

## Crítica constructiva

**Instrucciones:** La crítica constructiva puede ayudar a los demás a mejorar su trabajo. Usa estos comienzos de oraciones para hacer comentarios sobre el trabajo de tus compañeros.

#### Aclarar

¿Puedes explicar		?
------------------	--	---

¿Por qué decidiste \_\_\_\_\_?

¿Cómo hiciste para \_\_\_\_\_\_?

#### Comentarios cálidos

Me gusta \_\_\_\_\_\_ porque \_\_\_\_\_\_.

Es interesante que \_\_\_\_\_\_.

\_\_\_\_\_ es una buena idea porque \_\_\_\_\_.

#### **Comentarios tibios**

¿Has pensado en \_\_\_\_\_\_?

Me pregunto si \_\_\_\_\_\_\_.

Tal vez quieras intentar \_\_\_\_\_

Nombre:	Fecha:	

## Cubo: resultados de las pruebas

**Instrucciones:** Haz anotaciones y bosquejos de al menos 4 formas de vida que pasen por tu cubo. Tilda las casillas para indicar si el modelo de tu equipo cumplió con las limitaciones y los criterios de diseño.

Resultados de	e las pruebas	
Tiene las medidas correctas.	Resiste una caída desde 1 metro (3 pies) de altura.	
Es impermeable.	Se integra bien con el entorno.	
Observaciones		
	3.	
2.	4.	



Instrucciones: Relaciona la expresión con su forma correcta en palabras.

	1	
Expresión	Palabras	
1 4 × 3 ÷ 2	A Suma dos y tres. Multiplica la suma por cuatro.	
<b>2</b> (2 + 3) × 4	® Suma dos al producto de cuatro y tres.	
3 2 × (3 + 4)	© Duplica la suma de tres y cuatro.	
4 4 × 3 + 2	• Multiplica tres y cuatro. Divide entre dos.	
<b>1</b>	2	
3	4	

**Instrucciones:** Interpreta el significado de la siguiente expresión. Explica tu razonamiento.

<b>1</b> 4 × (3,489 + 2,149	5	4 × (3,489	+ 2,149
-----------------------------	---	------------	---------

Nombre: \_\_\_\_\_ Fecha: \_\_\_\_\_



Instrucciones: Responde las preguntas.

 $1 5 \times (9 - 3)$ 

Escribe la expresión con palabras.

Primero,\_\_\_\_\_

Después,\_\_\_\_\_\_.

Interpreta el significado de la expresión.

 $(6 + 4) \times 8$ 

Escribe la expresión con palabras.

Primero,\_\_\_\_\_\_\_.

Después,\_\_\_\_\_\_.

Interpreta el significado de la expresión.

\_\_\_\_\_

Elige la Pregunta 1 o la 2. Explica tu razonamiento.

# Día 4

## Tarea de aprendizaje continuo

**Instrucciones:** Responde las preguntas.

1  $2 \times \{4 + [(6 + 7) \times 3]\}$ 

Escribe la expresión con palabras.

Interpreta el significado de la expresión.

<b>2</b> {10 - [4 + (12 -	$\div 6)]$ × 4
---------------------------	----------------

Escribe la expresión con palabras.

Interpreta el significado de la expresión.

## Práctica independiente

Instrucciones: Escribe una expresión que coincida con las palabras.

- 1 Duplica la suma de diez y cuatro.
- 2 Resta dos de doce. Divide entre dos.
- 3 Seis menos la suma de ocho y cinco
- 4 Siete veces la diferencia de seis y cuatro

Instrucciones: Interpreta el significado de la expresión.

 $\mathbf{5} \ \ 34 \times (13,214 + 435)$ 

\_\_\_\_\_

**6**  $(40 + 35) \div 5$ 

\_\_\_\_\_

Nombre:	Fecha:
---------	--------



# Día doble para perros

Finnegan nunca se alejaba de su robusto bulldog llamado Big Mac. Un día, Finnegan estaba comprando en la tienda de mascotas Lucky Dog. Compró 5 bolsas de Mezcla Canina y 3 rosquillas para perros. El cajero dijo: "Hoy es tu día de suerte. ¡Es el día doble para perros! Te llevas el doble de premios sin tener que pagar más". Finnegan escribió una expresión para esta oferta:  $5+3\times 2$ . ¿Es correcta su expresión? ¿Por qué sí o por qué no?



Desarma el problema



Prepara un plan



Solución



Repasa y explica

